

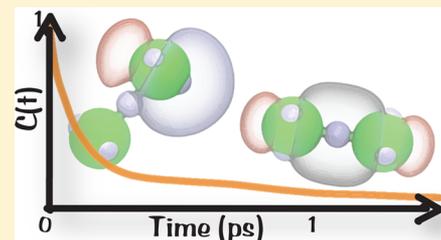
Halogen Bond Structure and Dynamics from Molecular Simulations

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Richard C. Remsing*¹ and Michael L. Klein*

Institute for Computational Molecular Science and Department of Chemistry, Temple University, Philadelphia, Pennsylvania 19122, United States

ABSTRACT: Halogen bonding has emerged as an important noncovalent interaction in a myriad of applications, including drug design, supramolecular assembly, and catalysis. The current understanding of the halogen bond is informed by electronic structure calculations on isolated molecules and/or crystal structures that are not readily transferable to liquids and disordered phases. To address this issue, we present a first-principles simulation-based approach for quantifying halogen bonds in molecular systems rooted in an understanding of nuclei–nuclei and electron–nuclei spatial correlations. We then demonstrate how this approach can be used to quantify the structure and dynamics of halogen bonds in condensed phases, using solid and liquid molecular chlorine as prototypical examples with high concentrations of halogen bonds. We close with a discussion of how the knowledge generated by our first-principles approach may inform the development of classical empirical models, with a consistent representation of halogen bonding.



INTRODUCTION

Noncovalent intermolecular interactions manifest the major driving forces in a wide variety of physicochemical processes. In this context, most attention has been focused on steric repulsion, hydrogen bonding, and van der Waals interactions. But in recent years, halogen bonding has emerged as a prominent interaction in many applications.^{1–6} A halogen bond is a directional attractive interaction between an electronegative region of one atom with an electropositive region of a halogen atom. The formation of this electropositive region is dependent on the polarizability of the halogen atom, such that their strength increases from F to Cl to Br to I to At,⁷ with F forming halogen bonds only in rare cases.

Halogen bonds have been successfully employed in crystal engineering^{4,8–10} and self-assembly^{3,11} and to tune reactivity in synthetic and catalytic applications.^{12–14} Recent work has demonstrated the utility of halogen bonds in solution,^{15,16} not only for self-assembly^{16,17} but also for anion binding with higher efficiency than hydrogen bonds.^{16,18,19} This selectivity of anions has been exploited to create highly active artificial ion channels.²⁰ Naturally occurring biomolecular halogen bonds are rare, with iodine-containing thyroid hormone-complexes as perhaps the best examples.^{21,22} More broadly, engineered biomolecular halogen bonds have also been exploited to enhance protein–ligand binding strengths^{23–25} and biomolecular self-assembly^{6,26} and promise to play an important role in the future of therapeutics.^{25,27}

Despite the importance and promise of halogen bonds in chemistry, biology, and materials science, an atomic level quantification is lacking. In this work, we use electronic structure calculations to develop a quantitative halogen bonding definition in condensed phases, using both nuclear and electronic correlations by exploiting maximally localized

Wannier functions.²⁸ We then employ *ab initio* molecular dynamics (AIMD) simulations and use this definition to analyze halogen bonding in solid and liquid Cl₂, model systems with a high concentration of halogen bonds (XBs). We also discuss how our results can inform the description of XBs within classical empirical models that are able to reach larger length and time scales than the AIMD simulations.

COMPUTATIONAL DETAILS

All calculations employed the CP2K package, and energies and forces were evaluated using the QUICKSTEP module.²⁹ QUICKSTEP employs basis sets of Gaussian-type orbitals and plane waves for the electron density, leading to an efficient and accurate implementation of DFT.³⁰ We employ the molecularly optimized (MOLOPT) Godecker–Teter–Hutter (GTH) triple- ζ , single polarization (TZVP-MOLOPT-GTH) basis set³⁰ and the GTH-PADE (LDA-based) pseudopotential³¹ to represent the core electrons. The valence electrons were treated explicitly, using the PBE³² or BLYP^{33,34} functionals as implemented in CP2K, or the SCAN functional^{35,36} as implemented in LibXC,^{37,38} with a plane wave cutoff of 400 Ry. The D3 van der Waals correction of Grimme et al. was employed with the PBE and BLYP functionals, as implemented in CP2K,³⁹ and the rVV10 van der Waals corrections parametrized for use with SCAN was employed to correct the SCAN functional.⁴⁰ Maximally localized Wannier functions (MLWFs) were obtained using CP2K, minimizing the spreads of the MLWFs according to the formulation of

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Equilibration to a constant temperature was achieved by using a Nosé–Hoover thermostat chain of length three^{42,43} with an integration time step of 1.0 fs. Systems were then further equilibrated in the microcanonical (NVE) ensemble for at least 10 ps, before gathering statistics over at least 4 ps of production simulation time. Simulations of liquid Cl₂ employed 72 molecules (144 atoms) and used periodic boundary conditions at the experimentally determined densities.⁴⁴ At 200 K, the cell dimensions are $L_x = 2.0867$ nm, $L_y = 1.49251$ nm, and $L_z = 1.84579$ nm, and at 300 K, $L_x = 2.39166$ nm, $L_y = 1.71063$ nm, and $L_z = 2.11554$ nm, where L_α is the length of the cell in the α -direction.

■ AB INITIO STRUCTURE AND DYNAMICS OF LIQUID CHLORINE

Before quantifying halogen bonding in condensed phases of Cl₂, we evaluate the ability of DFT-based approaches to predict the structure and dynamics of liquid chlorine (*l*-Cl₂). We first focus on the structure of *l*-Cl₂ as quantified by the radial distribution function, $g(r)$, shown in Figure 1 for $T = 200$ K and a density of $\rho = 12.5$ molecules/nm³, as obtained from simulations and experimental neutron diffraction measurements.⁴⁴ The position and height of the first major intermolecular peak in $g(r)$, as well as the first minimum, are best captured by the SCAN+rVV10 description of Cl₂, with SCAN and BLYP+D3 also providing a reasonable description

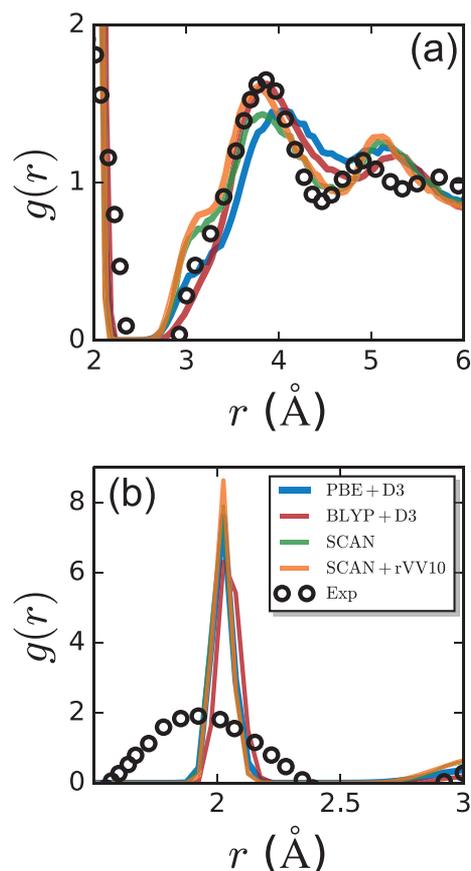


Figure 1. Radial distribution functions, $g(r)$, for Cl–Cl correlations in liquid Cl₂ at $T = 200$ K and $\rho = 12.5$ molecules/nm³ as determined by neutron scattering measurements⁴⁴ and four different density functional approximations. Both (a) intermolecular and (b) intramolecular correlations are shown.

of the liquid structure. The PBE+D3 functional shifts the first intermolecular peak to larger distances. All functionals yield a poor description of the second peak in $g(r)$. This is due to an overestimation of the Cl–Cl bond length; all estimate this distance above 2 Å, in contrast to the experimental bond length of 1.99 Å; see Figure 1b.

The simulated $g(r)$ displays a shoulder near 3 Å, the amplitude of which is dependent on the functional. As discussed in more detail in subsequent sections, this shoulder arises from halogen bonded dimers. Thus, the height of this shoulder is proportional to the strength of XBs in each system. The height of this shoulder, and consequently the XB strength, follows SCAN+rVV10 > SCAN > PBE+D3 > BLYP+D3. As compared with the experimental $g(r)$, SCAN+rVV10 and SCAN overestimate this shoulder, consistent with recent work showing that SCAN-based approaches can overestimate the strength of halogen bonds.⁴⁵ The PBE+D3 functional yields a reasonable description of the shoulder, despite a worse description of subsequent intermolecular correlations. BLYP+D3 underestimates the magnitude of this shoulder and, therefore, the strength of halogen bonds in this system.

Dynamic properties also provide a stringent test of *ab initio* predictions. In particular, we compare our predictions of the rotational time correlation function (TCF), $C_2(t)$, to experimental results, where

$$C_2(t) = \langle P_2(\mathbf{u}(t) \cdot \mathbf{u}(0)) \rangle \quad (1)$$

$P_2(x)$ is the second-order Legendre polynomial and $\mathbf{u}(t)$ is the Cl–Cl bond unit vector at time t . The rotational TCF $C_2(t)$ and its associated rotational correlation time τ_2 can be determined experimentally through Raman⁴⁶ and NMR spectroscopy.⁴⁷ We compare our predictions to results from Raman spectroscopy⁴⁶ in Figure 2.

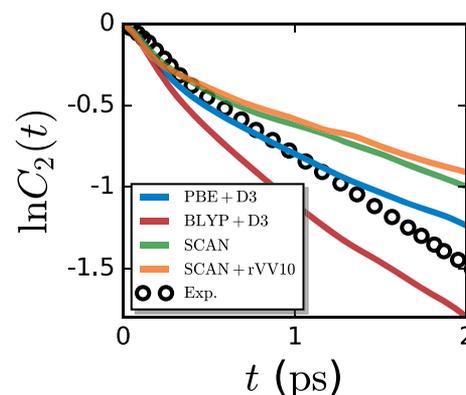


Figure 2. Rotational correlation function, $C_2(t)$, as determined through Raman spectroscopy (Exp)⁴⁶ and as predicted by the four density functional approximations used here. Experimental results were obtained at 198 K.

The rotational relaxation of *l*-Cl₂ is intimately tied to halogen bonding. In particular, if a chlorine dimer is halogen bonded with a neighbor, that XB must be broken in order for the dimer to rotate by a significant amount (ignoring the possibility of the pair rotating collectively with the bond intact). A similar rotational relaxation mechanism is known for water and other liquids with directional attractive interactions; i.e., H-bond breakage is involved in the rotational relaxation pathway of water.^{48,49} Thus, we expect rotational relaxation to

provide a sensitive, albeit indirect, probe of halogen bonding in $l\text{-Cl}_2$.

Indeed, the description of $C_2(t)$ provided by each functional closely tracks their respective ability to capture the shoulder in $g(r)$ at close distances assigned to halogen bonded dimers. The PBE+D3 functional yields an accurate description of the rotational dynamics of $l\text{-Cl}_2$, as described by $C_2(t)$. Both SCAN and SCAN+rVV10 yield rotational dynamics that are too slow, due the larger barrier to breaking XBs in these systems. The BLYP+D3 functional predicts a $C_2(t)$ that decays much too fast, consistent with the above conclusions that BLYP+D3 yields weaker XBs than expected.

Finally, we compute the vibrational density of states, $I(\omega)$, as the Fourier transform of the velocity autocorrelation $C_v(t)$, given by

$$C_v(t) = \frac{\langle \mathbf{v}(t) \cdot \mathbf{v}(0) \rangle}{\langle v^2(0) \rangle} \quad (2)$$

where $\mathbf{v}(t)$ is the velocity of an atom at time t and implicit in the ensemble average, $\langle \dots \rangle$, is an average over all atoms in the system. The vibrational density of states is show in Figure 3

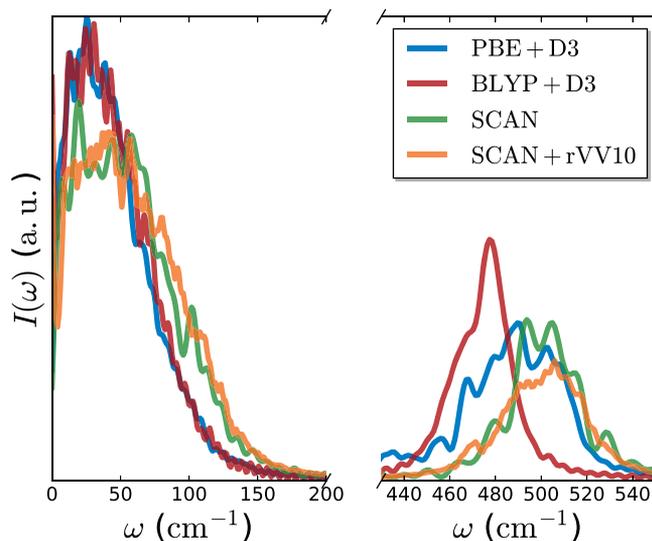


Figure 3. Vibrational density of states, $I(\omega)$, as predicted by the four density functional approximations used here.

and displays two main features, a high frequency peak and a low frequency peak. The high frequency peak corresponds to the Cl–Cl stretch vibration. All four functionals under study underestimate the frequency of the Cl–Cl stretch, which is experimentally between 530 and 550 cm^{-1} depending on the isotopic composition of the Cl_2 molecule.⁴⁶ This underestimation of the stretching frequency is consistent with each of the functionals predicting a Cl–Cl bond length that is too large, and the functional dependence of this peak position follows the bond lengths and their variances predicted by each functional; see Figure 5b.

The functionals display significant differences in the shape of the low frequency peak in $I(\omega)$; PBE+D3 and BLYP+D3 yield the same qualitative shape, while the SCAN-based functionals yield significantly more density at higher frequencies. The motions probed in this low frequency region of $I(\omega)$ involve collective rearrangements of the molecules in the liquid, which are dictated by breakage and reformation of XBs. Thus, we

ascribe these differences to the presence of stronger XBs in the SCAN-based functionals than PBE+D3 and BLYP+D3.

To summarize this section, we find that SCAN+rVV10 provides the best representation of the structure of $l\text{-Cl}_2$, at the cost of slowed dynamics. These slow dynamics arise from halogen bonds that are too strong, possibly due to self-interaction and/or density-driven errors.^{45,50,51} In contrast, the most accurate dynamics are predicted by PBE+D3, at the cost of a poorer overall description of $g(r)$. In the remainder of this work, we quantify the structure and dynamics of halogen bonding of Cl_2 . Because a major focus is on dynamic properties of XBs, data discussed throughout the remainder of the work is obtained using the PBE+D3 functional, and we make comparisons to the SCAN+rVV10 functional where appropriate.

■ ELECTRONIC STRUCTURE-BASED DEFINITION OF A HALOGEN BOND

Halogen bonding is the result of electrostatic attractions between regions of high and low electron density involving at least one halogen atom. In order to understand the origin of halogen bonds, we first examine the electronic structure of crystalline diatomic chlorine, whose crystal structure is a result of halogen bonding and packing of lone pairs.^{52–57}

In Figure 4, we show the maximally localized Wannier functions (MLWFs) for a single Cl_2 in the solid, where blue

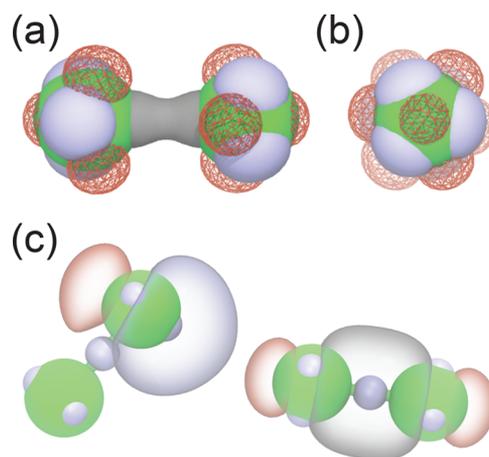


Figure 4. (a,b) Maximally localized Wannier functions (MLWFs) of a Cl_2 dimer in the solid state, shown from (a) the side and (b) down the Cl–Cl bond axis. The solid gray isosurface indicates the Cl–Cl covalent bond, and the solid blue isosurfaces indicate lone pairs; both are drawn at a value of 0.27 Bohr^{-3} . Red wireframe isosurfaces are opposite in sign to the solid surfaces and are drawn at a value of 0.09 Bohr^{-3} , chosen to be three times smaller than the isodensity contour used for the solid surfaces for clarity. Cl atoms are shown as green spheres. (c) MLWFs involved in a halogen bond (XB) between two chlorine dimers in the solid state. All isosurfaces are drawn at 0.05 Bohr^{-3} following the same color scheme as in panels a and b. Also shown are the centers of the MLWFs (MLWFCs) as small blue spheres. Note that an XB between two dimers is consistent with a linear Cl–Cl–MLWFC arrangement.

and red isosurfaces indicate regions of high and low electron density, respectively, and the covalent bond MLWF is highlighted in gray. In dimeric chlorine, bromine, and iodine, electron density is depleted along the covalent bond axis, leading to the formation of electron density deficient σ -holes at the ends of each dimer along the bond axis.^{55,57,58} Similar σ -

holes also develop between the lone pairs.^{57,58} These σ -holes can be readily observed as the wireframe regions of the MLWFs shown in Figure 4a,b.

A halogen bond forms when the lone pair region of one dimer forms a Lewis-type interaction with the σ -hole of a neighboring dimer.^{1,58} One such halogen bonding arrangement in crystalline Cl₂ is shown in Figure 4c, along with the corresponding MLWFs involved in the XB and all the MLWF centers (MLWFs) of the two dimers. The visualization in Figure 4c clearly indicates an electrostatic attraction between the electron rich portion of the lone pair MLWF of the left molecule (blue surface) with the electron deficient σ -hole of the right molecule (red surface). Moreover, Figure 4c suggests that halogen bonding is consistent with a linear Cl–Cl–MLWFC arrangement. Understanding the physical origin of XBs in this manner enables their quantification through a MLWF-based approach. In particular, we now introduce a geometric definition of a XB that is rooted in understanding the spatial correlations among Cl atoms and MLWFs.

The first component of our halogen bonding criterion is a Cl–Cl distance cutoff that defines a maximum distance for which two Cl atoms can be considered halogen bonded. The Cl–Cl radial distribution function, $g(r)$, shows a sharp peak at $r \approx 2$ Å that corresponds to the covalent bond in molecular chlorine, Figure 5a. The $g(r)$ then displays several peaks between $r \approx 3$ and 4.5 Å, the first of which is indicative of halogen-bonded Cl–Cl contacts. Thus, we define our distance cutoff based on the first minimum following this peak, such that $r_{\text{Cl–Cl}} < 3.4$ Å.

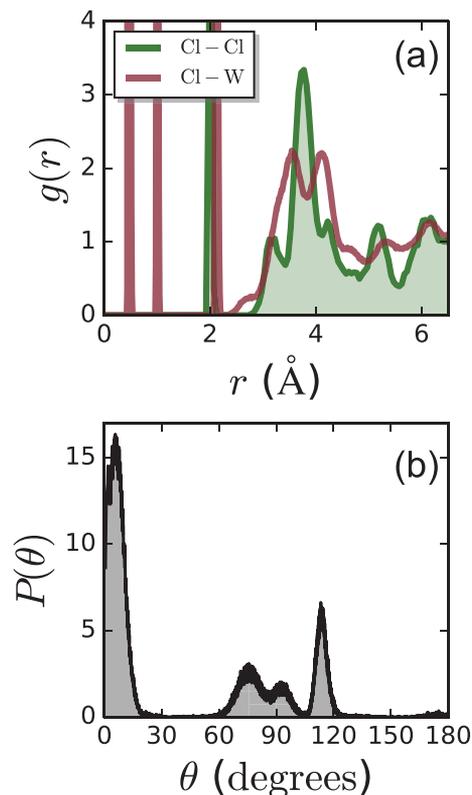


Figure 5. (a) Radial distribution function, $g(r)$, for Cl–Cl and Cl–W (Cl–MLWFC) correlations in solid Cl₂ at a temperature of 100 K. (b) Probability distribution of the Cl–Cl–W angle for MLWFs within a distance of 0.75 Å of a Cl atom.

We now include a second component of the geometric criterion for XBs that includes correlations involving MLWFs. The $g(r)$ characterizing correlations between MLWFs and Cl atoms (Cl–W, where W indicates a MLWFC) is also shown in Figure 5a. There are two types of MLWFs in Cl₂, lone pair and covalent bond MLWFs. The lone pair MLWFs correspond to the first peak in the Cl–MLWFC $g(r)$ near $r_{\text{Cl–W}} \approx 0.5$ Å, as well as the sharp peak near 2.1 Å. The covalent bond MLWFC contributes to the peak near 1 Å, roughly half the Cl–Cl bond length. The peak just before 3 Å is also consistent with lone pair MLWFs between two Cl atoms in a linear halogen bonding configuration.

A halogen bond is defined by a linear Cl–W...Cl arrangement, where the MLWFC (W) here corresponds to a lone pair. The probability distribution, $P(\theta)$, of the Cl–Cl–W angle, for MLWFs within a distance of 0.75 Å of a Cl atom, is shown in Figure 5b. The distribution $P(\theta)$ shows a large peak near $\theta = 0^\circ$, indicative of XBs. Additionally, there are peaks near 75° , 92° , and 115° , corresponding to MLWFs that are not involved in a XB with either of the Cl atoms in the Cl–Cl–W triplet. The sharp non-XB peak near $\theta = 115^\circ$ corresponds to MLWFs that are on the same Cl atom as the MLWFC involved in an XB. The remaining peaks correspond to MLWFs on the other Cl atom in the triplet, which is participating in the XB via a σ -hole.

We summarize our halogen bonding criterion as follows. A halogen bond between two Cl atoms exists if $r_{\text{Cl–Cl}} < 3.4$ Å and the Cl–Cl–W angle is $\theta < 30^\circ$, such that the MLWFC in the triplet corresponds to a lone pair, e.g. it is within 0.75 Å of one of the Cl nuclei. Examples of XBs in solid and liquid Cl₂ using our criterion are shown in Figure 6.

We note that our approach to halogen bonding is intended for condensed phases and may break down for isolated molecules or small clusters in vacuum. For an isolated Cl₂ molecule, its D_{∞h} symmetry leads to lone pair orientation being ill-defined. This symmetry manifests symmetric electrostatic potential surfaces around Cl-atoms of isolated molecules; for example, see refs 1, 5, 58, and 59. In the condensed phase, the environment surrounding a Cl₂ molecule provides an external potential that breaks this symmetry, resulting in well-defined lone pair orientations, observed in both the structure of MLWFs and electron densities.^{53,55,58} This symmetry breaking enables the use of MLWFs to robustly quantify XBs in condensed phases, as detailed in the following sections.

We conclude this section with a discussion of the robustness of our approach with respect to traditional XB definitions. Halogen bonds are often defined using nuclear coordinates only. In the case of a XB between two Cl₂ molecules, the halogen bond would be defined using the Cl–Cl intermolecular distance and the two angles formed by the Cl bond vectors and Cl–Cl intermolecular distance vector. While useful, such definitions include no information about the electronic structure of the system. By including information about the electronic degrees of freedom, our proposed definition is able to accurately and robustly characterize XBs in molecular systems, including situations where the purely nuclei-based definitions fail.

■ HALOGEN BONDS IN SOLID AND LIQUID CHLORINE

We can use the XB definition in the previous section to characterize the statistics of XBs in solid and liquid Cl₂. The

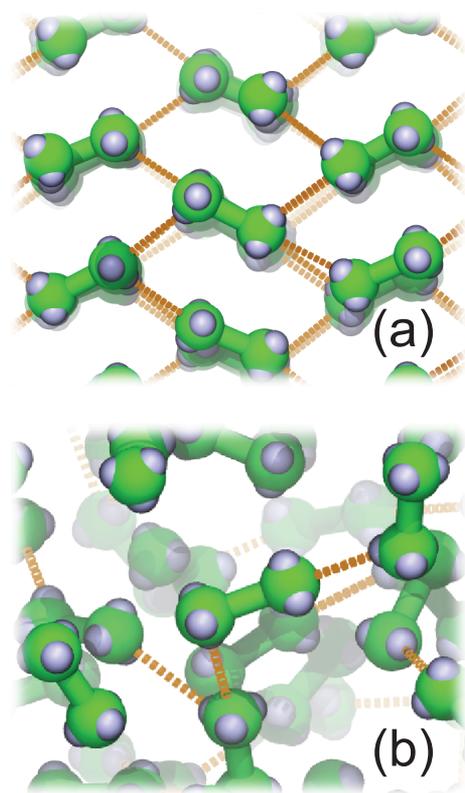


Figure 6. Snapshots illustrating halogen bonds in (a) solid and (b) liquid Cl_2 , at 100 and 200 K, respectively. Cl atoms are the large green spheres, MLWFCs are the small blue spheres, and halogen bonds are indicated by the orange dashed cylinders and identified according to the geometric criterion described in the text.

average number of XBs per molecule, $\langle n_{\text{XB}} \rangle$, is approximately 3.5 in the solid state; see Figure 7a. In the solid, each Cl atom can donate and accept a XB, as shown in Figure 6a, with thermal fluctuations transiently disrupting these interactions and reducing $\langle n_{\text{XB}} \rangle$ to 3.5, from the ideal value of 4.

The average number of XBs per molecule reduces to approximately 1.5 upon melting at 200 K, and further reducing to 1.3 at 300 K, as shown in Figure 7a. This reduction in halogen bonding is consistent with the lower density of the liquid—12.5 molecules/ nm^3 at 200 K and 8.32 molecules/ nm^3 at 300 K as compared to approximately 18 molecules/ nm^3 in the solid—as well as the increased rotational and translational dynamics of chlorine molecules.

We also examine the probability distribution of the number of XBs per molecule, $P(n_{\text{XB}})$, Figure 7b. In the solid state, $P(n_{\text{XB}})$ is peaked around $n_{\text{XB}} = 4$, consistent with the expectation that each Cl atom can donate and accept a XB in the orthorhombic arrangement of the solid. These XBs generally lead to the unique crystal structure of the larger halogen dimers, Cl_2 , Br_2 , and I_2 .^{54,55,57,58,60,61} As the temperature is increased along an isochore, the width of $P(n_{\text{XB}})$ increases, due to increased fluctuations of the crystal lattice, and the maximum shifts to $n_{\text{XB}} = 3$ in the superheated states, $T > 171$ K.

In the liquid state, $P(n_{\text{XB}})$ is peaked at $n_{\text{XB}} = 1$ and exhibits significant probability at values of n_{XB} between 0 and 4 XBs per molecule. The broad distribution of XBs in the liquid suggests that there is significant structural heterogeneity in $l\text{-Cl}_2$, which is not present in the solid state. This structural heterogeneity leads to broader distributions of observables, such as the larger

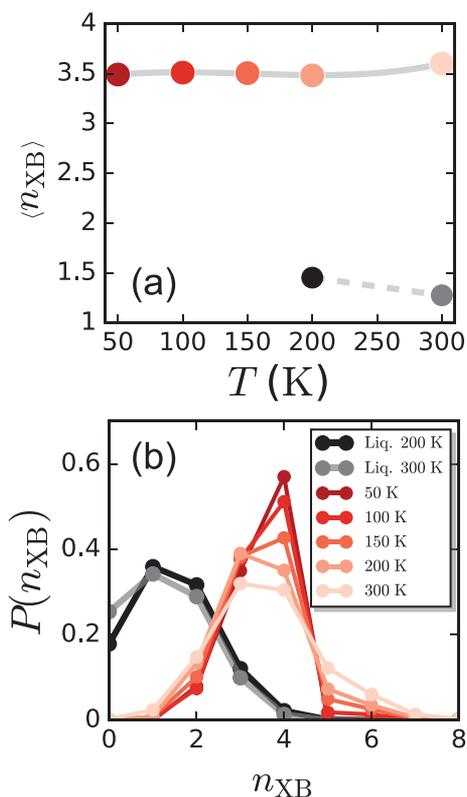


Figure 7. (a) Average number of halogen bonds per molecule, $\langle n_{\text{XB}} \rangle$, along an isochore in solid Cl_2 (points on solid line) and in liquid Cl_2 (points along dashed line). Lines are guides to the eye. (b) Probability distribution of the number of halogen bonds per molecule, $P(n_{\text{XB}})$, for the state points in panel a.

line width of the Cl–Cl stretching vibration peak in the Raman spectra of $l\text{-Cl}_2$, as compared to that of the solid.

■ HALOGEN BOND DYNAMICS IN CHLORINE

The MLWFC-based XB definition used here enables the characterization of XB dynamics. In particular, we define an indicator function, $h(t)$, which is equal to one when a XB exists at time t between two atoms and zero otherwise. Halogen bond dynamics can then be probed with the time correlation function (TCF)

$$C(t) = \frac{\langle h(t)h(0) \rangle}{\langle h \rangle} \quad (3)$$

in analogy with the procedure often used to probe hydrogen bonding dynamics.^{48,49,62–64}

The XB TCF is shown in Figure 8a for $l\text{-Cl}_2$ at 200 and 300 K. The decay of $C(t)$ can be fit by a biexponential decay with time scales of $\tau_1 \approx 0.08$ ps and $\tau_2 \approx 1.3$ ps at $T = 200$ K. We also compute the reactive flux correlation function^{62,63,65}

$$k(t) = -\frac{dC(t)}{dt} = -\frac{\langle \dot{h}(0)[1 - h(t)] \rangle}{\langle h \rangle} \quad (4)$$

which plateaus to a value of $k(t) \sim \tau^{-1} \exp(-t/\tau)$ after an initial transient period, as shown in Figure 8b. Indeed, fitting of $k(t)$ to the expected form in the plateau region yields a halogen bonding time scale of $\tau \approx 1.15$ ps at 200 K, in agreement with the biexponential decay of $C(t)$. The SCAN+rVV10 functional yields a longer XB lifetime, $\tau \approx 1.23$ ps at 200 K, consistent

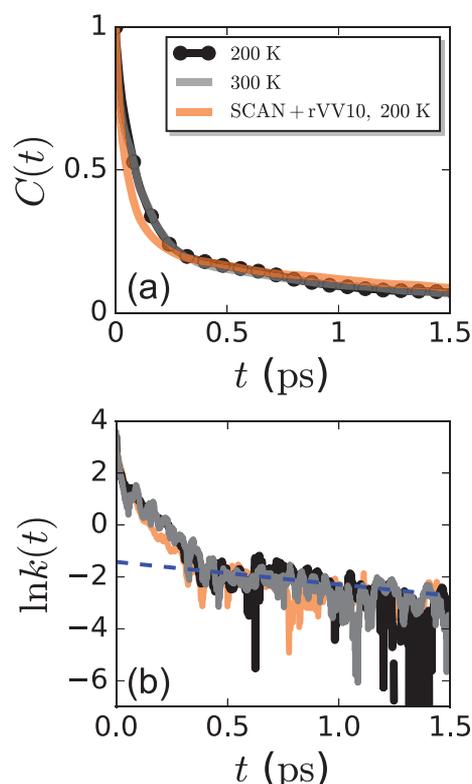


Figure 8. (a) Halogen bond time correlation function, $C(t)$, for liquid Cl_2 at 200 K (black) and 300 K (gray), as well as that predicted by SCAN+rVV10 at 200 K (orange). (b) Corresponding reactive flux correlation functions, $k(t)$, and a fit to $k(t) \sim \tau^{-1} \exp(-t/\tau)$ at long times (dashed lines), where τ is the halogen bond lifetime, is shown for the 200 K result.

with the stronger halogen bonds in this system, although the initial transient decay is faster than that predicted by PBE+D3.

At 300 K, the XB lifetime shortens to $\tau \approx 1.07$ ps, as may be expected from the increased dynamics at higher temperatures. The change in τ from 200 to 300 K closely tracks the change in the rotational relaxation time, $\tau_2 \approx 1.13$ ps at 200 K and $\tau_2 \approx 1.07$ ps at 300 K, as determined by fitting the long-time behavior of $C_2(t)$ to an exponential decay. This correlation between τ and τ_2 supports the earlier suggestion that a significant pathway for rotational relaxation in $l\text{-Cl}_2$ involves XB breakage. We additionally note that the XB lifetime in $l\text{-Cl}_2$ in this temperature range is on the order of a picosecond, similar to the lifetime of hydrogen bonds in water at ambient conditions.^{62,63}

The computation of $C(t)$ shown here demonstrates that dynamic properties of XBs can be readily evaluated using our approach. For example, the time-dependence of XBs in contexts such as halogenated ligand unbinding from proteins and phase transitions in supramolecular assemblies can be readily quantified and halogen bonding rate constants can be computed. These concepts will shed light on the role of XBs in determining the kinetics of a wide array of processes in the chemical, material, and biological sciences.

CONCLUSIONS

In this work, we have used *ab initio* molecular dynamics simulations in combination with the maximally localized Wannier function formalism to characterize the structure and dynamics of condensed phase halogen bonds on a footing

equal to traditional measures of hydrogen bonding. This consistent picture of noncovalent, directional interactions enables extension of the vast literature on hydrogen bonding in molecular systems to characterize halogen bonding. The general approach used here can be extended to bromine and iodine-containing systems, using two- and three-body correlations among nuclei and MLWFCs to develop halogen bonding criteria for Br–Br and I–I XBs. Analogously, the approach may also be extended for heteroatom XBs, and future work will focus on these extensions.

We close with a discussion of how our results may be used to develop classical, empirical models of halogen bonding, which will enable molecular simulations on larger length and time scales. Such models will be important for describing halogen bonding in supramolecular assemblies and protein–ligand complexes, for example, especially if dynamic and thermodynamic properties are of interest. We expect that an empirical model of halogen bonding in Cl_2 can be developed from first-principles using the insights provided by our XB analysis scheme. In particular, one might imagine constructing a semirigid, 8-site model of Cl_2 , wherein each Cl atom is represented by four sites, one Cl nucleus, and three lone pair sites (LPs). This differs from recently developed empirical models of halogen bonding in that the lone pair sites are explicitly represented.^{66–68} Bond lengths and angles involving Cl and LP sites could be determined from AIMD averages, and the charges on the LP and Cl sites may be chosen to reproduce the quadrupole moment of the Cl_2 molecule, or tuned to match the structure of condensed phase Cl_2 more accurately. Alternately, the intermolecular interactions could be developed through machine learning approaches applied to *ab initio* computations of the type reported herein.^{69,70} Moreover, we expect such empirical representations of halogen bonding to be transferable to halogenated compounds in general, including organic crystals and biomolecular systems.

AUTHOR INFORMATION

Corresponding Authors

*E-mail: rremsing@temple.edu (R.C.R.).

*E-mail: mlklein@temple.edu (M.L.K.).

ORCID

Richard C. Remsing: 0000-0002-0922-4882

Notes

The authors declare no competing financial interest.

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